

EXAMINATION 2 ANSWER KEY

“Consumers and Demand”

Version A

I. Multiple choice

(1)b . (2)d. (3)a. (4)c. (5)b. (6)b. (7)a. (8)c. (9)c. (10)b.

II. Short answer

- | | | | |
|-----|-----------------------------------------------------------------------------------------------------------|---------------------------------------------------------------|---------------------------------|
| (1) | a. elastic.
d. decrease. | b. decrease.
e. 2 %. | c. 6 %. |
| (2) | a. necessary good.
d. decrease. | b. increase.
e. 8 %. | c. 2 %. |
| (3) | Note: This graph is based on Slutsky’s approach to income and substitution effects, not Hicks’s approach. | | |
| | a. \$4.
d. 3 units energy. | b. 10 units energy.
e. -5 units energy. | c. \$10.
f. -2 units energy. |
| (4) | a. $\epsilon^{\text{comp}} = -1.02$.
d. decrease | b. decrease.
e. 10.02 % (using ϵ^{comp}). | c. 11 % (using ϵ). |
| (5) | a. Laspeyres = 140. | b. Paasche = 130. | c. $\sqrt{140 \times 130}$. |

III. Problems

- (1) [Budgets and choice]
 a. Equation for budget line (income=spending): $160 = 5 q_1 + 4 q_2$.
 b. $\text{MRSC} = \text{MU}_2/\text{MU}_1 = (q_1-8) / q_2$.
 c. Solve the tangency condition [$\text{MRSC} = p_2/p_1$ or $(q_1-8) / q_2 = 4/5$] jointly with equation for budget line (see part a) to get $q_1^* = 20$, $q_2^* = 15$.
- (2) [Properties of individual demand functions]
 a. Homogeneity of degree zero means that if income and all prices are multiplied by the same factor, the quantity demanded never changes. Check homogeneity of the demand function by replacing I by (aI) , replacing p_1 by (ap_1) , and replacing p_2 by (ap_2) , where a is an arbitrary factor:

$$\begin{aligned}
 & 2 (aI)^{1.5} (ap_1)^{-0.5} (ap_2)^{0.1} \\
 &= a^{1.5-0.5+0.1} 2 I^{1.5} p_1^{-0.5} p_2^{0.1} \\
 &= a^{1.1} 2 I^{1.5} p_1^{-0.5} p_2^{0.1}
 \end{aligned}$$

Note that the “a” factor does *not* cancel. So multiplying income and prices by some arbitrary positive factor a changes the quantity demanded. This function is not homogeneous of degree zero in income and prices.

- b. $\frac{\partial q_1^*}{\partial p_1} = 2 I^{1.5} (-0.5) p_1^{-1.5} p_2^{0.1}$. This expression is negative, so good #1 is an ordinary good, not a Giffen good.
- c. $\frac{\partial q_1^*}{\partial I} = 2 (1.5) I^{0.5} p_1^{-0.5} p_2^{0.1}$. This expression is positive, so good #1 is a normal good, not an inferior good.
- d. $\frac{\partial q_1^*}{\partial p_2} = 2 I^{1.5} p_1^{-0.5} (0.1) p_2^{-0.9}$. This expression is positive, so goods #1 and #2 are substitutes, not complements.
- (3) [Finding individual demand functions]
- a. $MRS = MU_2/MU_1 = (q_1^2 5q_2^4) / (2 q_1 q_2^5) = (5q_1) / (2q_2)$.
- b. Solve $MRS = (5q_1) / (2q_2) = p_2/p_1$ (the tangency condition) jointly with $I = p_1 q_1 + p_2 q_2$ (the budget constraint) to get $q_1^* = \frac{2I}{7 p_1}$, and
- c. $q_2^* = \frac{5I}{7 p_2}$.
- [There are many ways to solve the equations jointly. One way to begin is to cross-multiply the tangency condition to get $(5/2) p_1 q_1 = p_2 q_2$. Then substitute into the budget constraint:
- $$I = p_1 q_1 + (5/2) p_1 q_1 = (7/2) p_1 q_1 .$$
- Then solve for q_1^* as a function of p_1 and I . Finally, substitute your expression for q_1^* into either the budget constraint or the tangency condition and solve for q_2^* as a function of p_2 and I . These particular demand functions depend on income and the own price of the good—they do not depend on the price of the other good. This always happens with Cobb-Douglas utility functions, so you would not want to use a Cobb-Douglas utility function to model substitutes and complements.]

IV. Critical thinking

- (1) Demand for this good is **inelastic** because spending rises when the price increases. To compute the price elasticity of demand, recall that for small percent changes,
- $$\% \text{ change spending} = \% \text{ change price} + \% \text{ change quantity}$$
- Substituting the numbers given in the problem:
- $$7\% = 10\% + \% \text{ change quantity}$$
- So the percent change in quantity is -3%. The price elasticity of demand by definition equals percent change in quantity divided by percent change in price = $-3\%/10\% = -0.3$.
- (2) This good must be a **luxury (or superior) good** because the spending share rises when income rises. To compute the income elasticity of demand, recall that for small percent changes,
- $$\% \text{ change spending share} = \% \text{ change quantity} - \% \text{ change income}$$
- Substituting the numbers given in the problem:
- $$2\% = \% \text{ change quantity} - 5\%$$
- So the percent change in quantity is 7%. The income elasticity of demand by definition equals percent change in quantity divided by percent change in income = $7\%/5\% = 1.4$.

Version B

I. Multiple choice

(1)c. (2)b. (3)e. (4)b. (5)d. (6)c. (7)b. (8)d. (9)c. (10)d.

II. Short answer

- (1) a. inelastic. b. decrease. c. 2 %.
d. increase. e. 3 %.
- (2) a. luxury or superior good. b. increase. c. 6 %.
d. increase. e. 1 %.
- (3) Note: This graph is based on Slutsky's approach to income and substitution effects, not Hicks's approach.
a. \$2. b. 10 units of food. c. \$8.
d. 2 units of food. e. -6 units of food. f. -2 units of food.
- (4) a. $\epsilon^{\text{comp}} = -0.53$. b. decrease. c. 8 % (using ϵ).
d. decrease e. 5.3 % (using ϵ^{comp}).
- (5) a. Laspeyres = 160. b. Paasche = 130. c. $\sqrt{160 \times 130}$.

III. Problems

- (1) [Budgets and choice]
a. Equation for budget line (income=spending): $150 = 5 q_1 + 6 q_2$.
b. $\text{MRSC} = \text{MU}_2/\text{MU}_1 = q_1 / (q_2 - 5)$.
c. Solve the tangency condition [$\text{MRSC} = p_2/p_1$ or $q_1 / (q_2 - 5) = 6/5$] jointly with equation for budget line (see part a) to get $q_1^* = 12$, $q_2^* = 15$.
- (2) [Properties of individual demand functions]
a. Homogeneity of degree zero means that if income and all prices are multiplied by the same factor, the quantity demanded never changes. Check homogeneity of the demand function by replacing I by (aI) , replacing p_1 by (ap_1) , and replacing p_2 by (ap_2) , where a is an arbitrary factor:

$$\begin{aligned} & (aI - 2ap_2)(ap_1)^{-1} + 3 \\ &= a a^{-1} (I - 2p_2)(p_1)^{-1} + 3 \\ &= (I - 2p_2)(p_1)^{-1} + 3 \end{aligned}$$

Note that the "a" factor cancels. So multiplying income and prices by some arbitrary positive factor a *does not* change the quantity demanded. The function IS homogeneous of degree zero in income and prices.

- b. $\frac{\partial q_1^*}{\partial p_1} = (I - 2p_2)(-1)(p_1)^{-2}$. This expression is negative, so good #1 is an ordinary good, not a Giffen good.
- c. $\frac{\partial q_1^*}{\partial I} = (p_1)^{-1}$. This expression is positive, so good #1 is a normal good, not an inferior good.

- d. $\frac{\partial q_1^*}{\partial p_2} = -2(p_1)^{-1}$. This expression is negative, so goods #1 and #2 are complements, not substitutes.
- (3) [Finding individual demand functions]
- a. $MRS = MU_2/MU_1 = (4 q_1^3 q_2^3) / (3 q_1^2 q_2^4) = (4q_1) / (3q_2)$.
- b. Solve $MRS = (4q_1) / (3q_2) = p_2/p_1$ (the tangency condition) jointly with $I = p_1 q_1 + p_2 q_2$ (the budget constraint) to get $q_1^* = \frac{3I}{7p_1}$, and
- c. $q_2^* = \frac{4I}{7p_2}$.
- [There are many ways to solve the equations jointly. One way to begin is to cross-multiply the tangency condition to get $(4/3) p_1 q_1 = p_2 q_2$. Then substitute into the budget constraint:
- $$I = p_1 q_1 + (4/3) p_1 q_1 = (7/3) p_1 q_1 .$$
- Then solve for q_1^* as a function of p_1 and I . Finally, substitute your expression for q_1^* into either the budget constraint or the tangency condition and solve for q_2^* as a function of p_2 and I . These particular demand functions depend on income and the own price of the good—they do not depend on the price of the other good. This always happens with Cobb-Douglas utility functions, so you would not want to use a Cobb-Douglas utility function to model substitutes and complements.]

IV. Critical thinking

Same as Version A.

[end of answer key]