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EXAMINATION #2 VERSION A
"Consumers and Demand"
September 30, 2021

INSTRUCTIONS: This exam is closed-book, closed-notes. Calculators, mobile phones, and wireless devices are NOT permitted. Point values for each question are noted in brackets.

I. MULTIPLE CHOICE: Circle the one best answer to each question. Use margins for scratch work. [1 pt each—10 pts total]

(1) According to the assumption of "monotonicity" or "more is better," which bundle in the graph below *must* be preferred by any consumer to bundle X?
a.   Bundle A only.
b.   Bundle B only.
c.   Bundle C only.
d.   All of the above.
e.   None of the above.
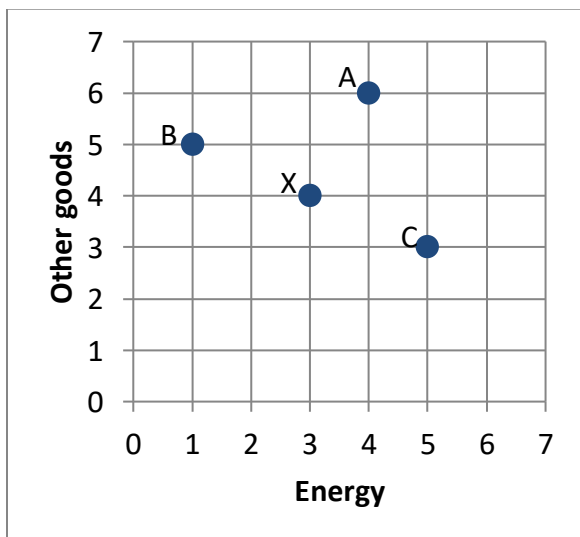
(2) Which utility function below violates the assumption of "diminishing marginal rate of substitution"?
a. $U(q_1,q_2) = q_1^2 q_2^3$.
b. $U(q_1,q_2) = (q_1+2)(q_2+3)$.
c. $U(q_1,q_2) = 2q_1 + 3q_2$

(3) In the graph below, the shift in the budget line could be caused by
a.   an increase in income.
b.   a decrease in income.
c.   an increase in the price of entertainment.
d.   a decrease in the price of entertainment.
e.   an increase in the price of other goods.
f.   a decrease in the price of other goods.
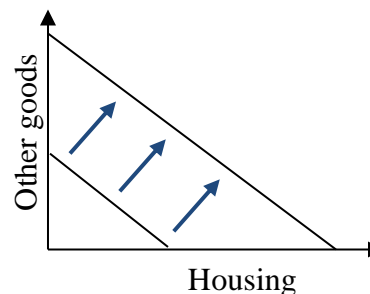
The next two questions refer to the following graph of a consumer's budget line and indifference curves. Suppose the consumer is currently at bundle A for some reason.
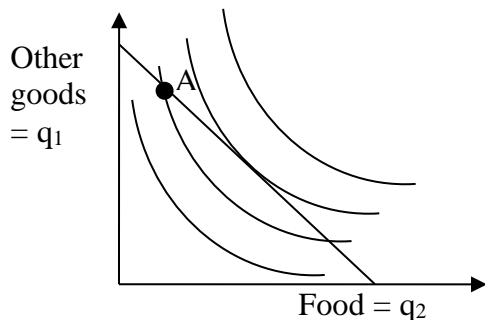
(4) This consumer could enjoy higher utility, without increasing total spending, by
a. purchasing less food and more other goods.
b. purchasing more food and fewer other goods.
c. purchasing less food and fewer other goods.
d. any of the above.
e. none of the above.

(5) Let MU_1 denote the marginal utility of other goods and MU_2 the marginal utility of food for this consumer. Let p_1 denote the price of other goods and p_2 denote the price of food. At bundle A,
a. $MU_2 = MU_1$ and $p_2 = p_1$.
b. $MU_2/MU_1 = p_2/p_1$.
c. $MU_2/MU_1 < p_2/p_1$.
d. $MU_2/MU_1 > p_2/p_1$.
e. cannot be determined from information given.

(6) Which of the following demand functions exhibits a constant price elasticity of demand?
a. $q_1{}^* = 5\ p_1{}^{-1.2}\ I^{1.1}\ p_2{}^{0.2}$.
b. $q_1{}^* = I/(6p_1) + 3$.
c. $q_1{}^* = 50 - 2\ p_1 + 0.08\ I - 0.01\ p_2$.

(7) Which price index tends to overestimate the rate of inflation?
a. Laspeyres price index.
b. Paasche price index.
c. Fisher price index.
d. All of the above.
e. None of the above.

(8) As one moves along an *ordinary* demand curve (sometimes called a "Marshallian" demand curve) for a particular good, the
a. price of the good is held constant.
b. quantity demanded of the good is held constant.
c. the consumer's income is held constant.
d. the consumer's utility is held constant.
e. none of the above.

The next two questions refer to the following graph of ordinary and compensated demand curves for pumpkins.

Legend:
— Ordinary demand
— Compensated demand
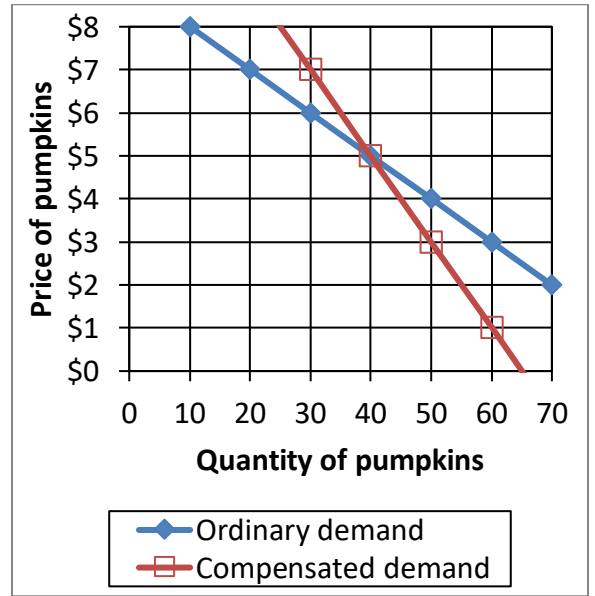
(9) Suppose the price of pumpkins fell from $5 to $3. The decrease in income that would exactly compensate consumers for this fall in price, leaving consumers just as well off as before the price change, would be

a. $2.
b. $80.
c. $90.
d. $100.

(10) Again suppose the price of pumpkins fell from $5 to $3. The increase in consumer surplus would be

a. $2.
b. $80.
c. $90.
d. $100.

II. SHORT ANSWER: Please write your answers in the boxes on this question sheet. Use margins for scratch work.

(1) [Price elasticity of demand: 10 pts] Suppose the price elasticity of demand for coffee is –0.25, and the price of coffee rises by 8 %.

a. Is the demand for coffee *elastic* or *inelastic* ?

b. Will the quantity demanded of coffee *increase* or *decrease*?

c. By about how much?   %

d. Will consumers' total spending on coffee *increase* or
    decrease?

e. By about how much?   %

(2) [Income elasticity of demand: 10 pts] Suppose that a consumer's income rises by 4%, and the income elasticity of demand for concert tickets is 1.25 .

a. Does the income elasticity indicate that concert tickets are an
    inferior good, a *necessary* good, or a *luxury or superior* good?

b. Will the quantity demanded of concert tickets *increase* or
    decrease?

c. By about how much?   %

d. Will the share of the consumer's budget devoted to concert
    tickets *increase* or *decrease*?

e. By about how much?   %

(3) [Substitution and income effects: 12 pts] Consider the indifference-curve diagram below.
Assume the consumer has $60 income.
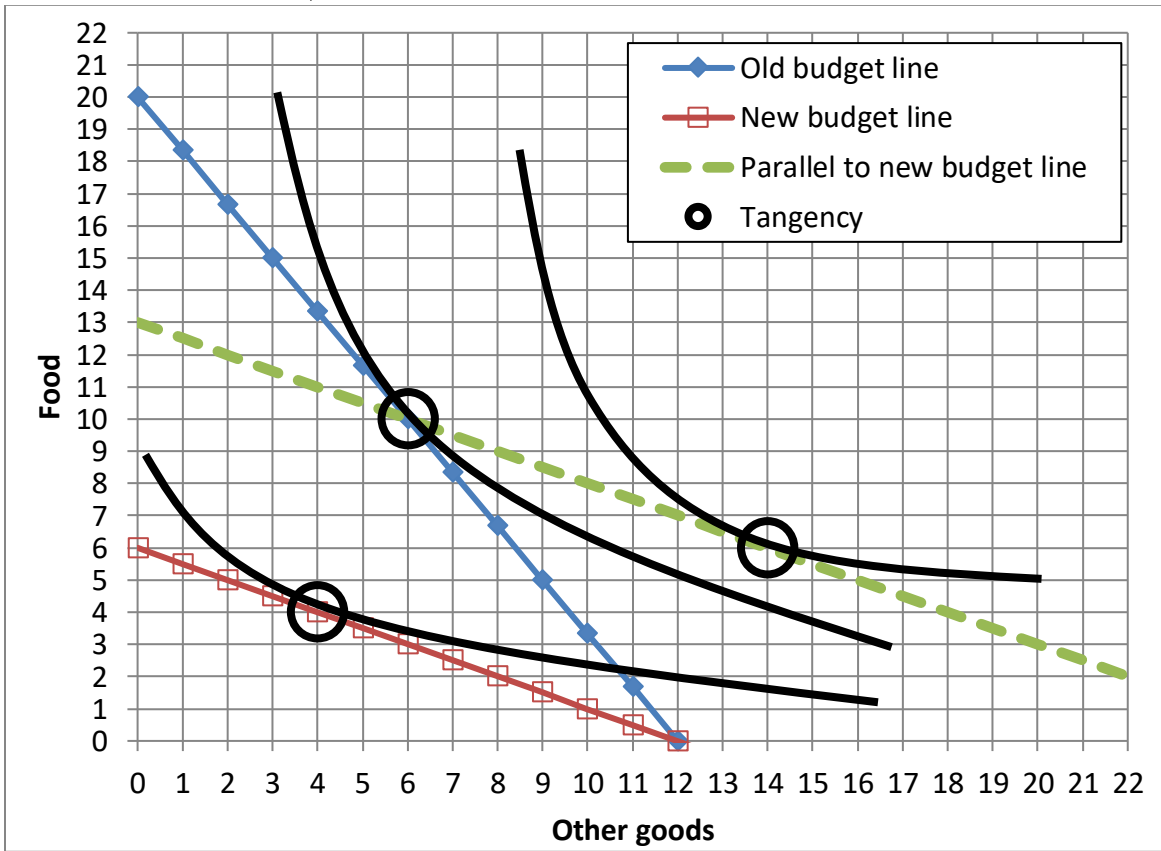
a. What was the price of a unit of food on the old budget line?

$

b. Given the old budget line, how many units of food does the consumer demand?

units

c. What is the price of a unit of food on the new budget line?

$

d. Given the new budget line, how many units of food does the consumer demand?

units

e. Compute the *change* in quantity of food demanded due to the substitution effect: Δq^{sub} .

units

f. Compute the *change* in quantity of food demanded due to the income effect: Δq^{inc} .

units

(4) [Slutsky equation: 10 pts] The Slutsky equation in elasticity form is given by

$$\varepsilon = -S\,\eta + \varepsilon^{comp}$$

where, as usual, ε denotes the own-price elasticity of demand, S denotes the share of total consumer spending devoted to the good (a fraction), η denotes the income elasticity of demand, and ε^{comp} denotes the compensated demand elasticity. Suppose that for food, $\varepsilon = -0.25$, $S = 0.15$, and $\eta = 0.4$.
 a. Compute the compensated demand elasticity (ε^{comp}).

Suppose the price of food rises by 10%, but the consumer's income does *not* change.
 b. Does the quantity demanded of food *increase* or *decrease*?

 c. By about how much?   %

Continue to assume that the price of food rises by 10%, but now suppose the government helps the consumer by giving them a cash transfer equal to 10% of last year's spending on food.
 d. Does the quantity demanded of food *increase* or *decrease*?

 e. By about how much?   %

(5) [Cost-of-living indexes: 6 pts] Suppose we are given the following data on prices and quantities consumed of food and other goods.

	Food		Other goods	
	Price	Quantity	Price	Quantity
Old period	$3	10 units	$5	4 units
New period	$5	5 units	$5	7 units

Assume that all cost-of-living indexes equal 100 in the old period.
 a. Compute the *value* of the Laspeyres cost-of-living index in the new period.
 b. Compute the *value* of the Paasche cost-of-living index in the new period.
 c. Give a *formula* for the Fisher cost-of-living index in the new period. The formula should include numbers but no variables.

III. PROBLEMS: Please write your answers in the boxes on this question sheet. Show your work and circle your final answers.

(1) [Budgets and choice: 14 pts] A consumer has the following utility function:

$U(q_1, q_2) = q_1^{1/2} + q_2^{1/2}$, where q_1 denotes the slices of pizza and q_2 denotes the quantity of other goods. The price of slices of pizza is $3 and the price of other goods is $2. The consumer has $60 in income to spend on these items.

   a. [4 pts] Give an equation for the consumer's budget line. The variables q_1 and q_2 should be the only unknowns.

   b. [4 pts] Find a formula for the consumer's marginal rate of substitution in consumption of other goods for pizza—that is, the |slope| of the consumer's indifference curve with slices of pizza on the vertical axis and other goods on the horizontal axis. The variables q_1 and q_2 should be the only unknowns. Circle your final answer.

   c. [6 pts] Solve for the slices of pizza (q_1^*) and other goods (q_2^*) that this consumer will choose. Circle your final answers.

(2) [Properties of individual demand functions: 12 pts] Suppose an alleged demand function is
$$q_1^* = 5 \; p_1^{-0.8} \; I^{1.2} \; p_2^{0.1} \;,$$ where I denotes the consumer's income, p_1 denotes the price of good #1, and p_2 denotes the price of good #2.

   a.   Is this function homogeneous of degree zero in income and prices? Justify your answer.

   b.   Find the partial derivative $\partial q_1^*/\partial p_1$. Is good #1 an ordinary good or a Giffen good? Justify your answer.

   c.   Find the partial derivative $\partial q_1^*/\partial I$. Is good #1 an inferior good or a normal good? Justify your answer.

   d.   Find the partial derivative $\partial q_1^*/\partial p_2$. Are goods #1 and #2 substitutes, complements, or unrelated in demand? Justify your answer.

(3) [Finding individual demand functions: 12 pts] A consumer has the following utility function:
$U(q_1, q_2) = q_1 q_2^2$, where q_1 denotes the quantity of entertainment and q_2 denotes the quantity of other goods.

a. Find a formula for the consumer's marginal rate of substitution in consumption of other goods for entertainment—that is, the |slope| of the consumer's indifference curve with entertainment on the vertical axis and other goods on the horizontal axis. The variables q_1 and q_2 should be the only unknowns. Circle your final answer.

Let p_1 denote the price of entertainment and let p_2 denote the price of other goods. Let I denote the consumer's income.

b. Solve for the consumer's demand function for entertainment—that is, the formula showing q_1* as a function of p_1, p_2, and I (but not q_2). Show your work and circle your final answer. [Hint: check that your answer is homogeneous of degree zero.]

c. Solve for the consumer's demand function for other goods—that is, the formula showing q_2* as a function of p_1, p_2, and I (but not q_1). Show your work and circle your final answer. [Hint: check that your answer is homogeneous of degree zero.]

IV. CRITICAL THINKING: Answer just *one* of the questions below (your choice). [4 pts]

(1) Ana's utility function is $U = q_1 q_2$, where q_1 denotes the quantity of food and q_2 denotes the quantity of other goods. Suppose the price of food is $p_1 = \$3$ and the price of other goods is $p_2 = \$4$. Compute the *minimum* amount of income that Ana must have to attain a target level of utility of $U = 300$ utils. Show your work and circle your final answer.

(2) Suppose Bob buys only sandwiches (q_s) and Gatorade (q_g). Suppose the prices of both items double from the old period to the new period. That is,
$$p_s^{new} = 2\ p_s^{old} \qquad \text{and} \qquad p_g^{new} = 2\ p_g^{old}.$$
(However, we do not know what quantities Bob chooses in either period.) Which increases faster—Bob's *Laspeyres* cost-of-living index, his *Paasche* cost-of-living index, or his *Fisher* cost-of-living index? Justify your answer using algebra.

Circle the question you are answering and write your answer below. Full credit requires good grammar, legible writing, accurate spelling, and correct reasoning.

[end of exam]